

INVESTIGATION OF THERMAL PERFORMANCE OF AIR TO WATER HEAT EXCHANGER USING NANO-FLUIDS

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ABSTRACT: In the present study the three-dimensional numerical simulation is selected as a tool to investigate the effectiveness of a cross flow heat exchanger. Water is selected to be mixed with nano-particles and flow inside a circular pipe while a pure air is flowing across it. Numerical simulations is carried out under laminar flow for both water and air sides. The thickness of the pipe is neglected in the present preliminary study. From the physics of the problem, the governing parameters can be determined as: the Reynolds, the type and the volume fraction of the nano-fluid. The effect of these governing parameters is studied and the results are presented. The results show significant enhancement of heat transfer with introduction of nano-particles, such as titanium-oxide (TiO₂) nano-powder, compared to the pure base fluid. The accuracy of the results presented in the present study depends on the accuracy of the effective properties of the nano-fluids, which are taken from the open literature.

ABSTRAK: Dalam kajian ini, simulasi tiga dimensi berangka digunakan untuk mengkaji keberkesanan penukar haba aliran silang. Air dipilih untuk dicampurkan dengan zarah bersaiz nano dan dialirkan di dalam paip berbentuk bulat, sementara udara tulen mengalir melaluinya. Simulasi berangka dijalankan di bawah aliran lamina untuk kedua-dua belah air dan udara. Ketebalan paip diabaikan di dalam kajian permulaan ini. Dari sudut permasalahan fizik, parameter pengawal imbang boleh ditentukan sebagai: nombor Reynolds, jenis dan isipadu pecahan bendalir nano. Kesan parameter pengawal imbang ini dikaji dan keputusannya dibentangkan. Keputusan menunjukkan peningkatan pemindahan haba yang ketara dengan penggunaan zarah bersaiz nano seperti serbuk titanium oksida (TiO₂), berbanding dengan bendalir tulen. Ketepatan keputusan kajian ini bergantung kepada ketepatan sifat-sifat efektif bendalir nano yang dirujuk daripada sumber maklumat terdahulu.

KEYWORDS: *heat exchanger; nanofluids; effective thermal properties*

1. INTRODUCTION

It is well known that metals in solid form have thermal conductivities that are higher than fluids. For example, thermal conductivity of copper at room temperature is about 700 times greater than that of water. Even oxides such as alumina (Al₂O₃), titanium oxide (TiO₂) which are good insulators compared to metals have high thermal conductivities compared to water [1]. Conventionally, when heat transfer fluids do not have the capacity to cool the mechanical

machinery fast enough, an alternative is to use a metallic solid with several times the heat transfer capacity of the base fluid as a heat dissipating medium. In conventional cases, the suspended particles are of micrometer or even millimeter dimensions. This can give higher heat transfer rates, compared with common base fluids, but the large suspended particles in the fluid present problems such as sedimentation of particles, erosion of channel walls, fouling and increased pressure drop in the flow channel [2]. Therefore, fluids with large suspended particles have little practical application in enhancing heat transfer process. In comparison, nano-particles submerged in fluids (termed nanofluids) are more desirable because of their considerably smaller size, better stability and rheological properties, and higher thermal conductivities compared with microfluids, and there is no penalty in pressure drop [3]. Besides that, nanofluids are also very stable and have no additional problems, such as sedimentation, erosion, additional pressure drop and non-Newtonian behaviour due to tiny size of nanoelements and low volume fraction of nanoelements required. Investigations on adding nano-particles to the base fluid to enhance heat transfer have been carried out by many researchers [4-10] either experimentally or by numerical simulation. In these studies, they concluded that nanoparticles can remarkably enhance the thermal performance of base fluids by about 20-30%. The present paper is considering the numerical simulation investigation of the thermal performance of the air to water heat exchanger in cross flow using nanofluids.

2. MATHEMATICAL MODEL

The mathematical model in the present study is using single phase model with the assumption that the nanofluid is single and continuous fluid phase. Parameters such as density, thermal capability, thermal conductivity and viscosity are varied in single phase flow. The governing equations are:

Conservation of mass (Continuity equation)

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \quad (1)$$

Conservation of momentum (Navier-Stokes equation)

$$\rho_{nf} \left(u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right) = -\frac{dp}{dx} + \mu_{nf} \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) \quad (2)$$

$$\rho_{nf} \left(u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} \right) = -\frac{dp}{dy} + \mu_{nf} \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right) \quad (3)$$

$$\rho_{nf} \left(u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} \right) = -\frac{dp}{dz} + \mu_{nf} \left(\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) \quad (4)$$

Conservation of energy

$$\rho_{nf} C_{p,nf} \left(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} \right) = k_{nf} \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) \quad (5)$$

where u, v, w (m.s^{-1}) are the velocity components in the x, y and z direction respectively, ρ_{nf} (kg.m^{-3}) is density of nanofluid, μ_{nf} ($\text{kg.m}^{-1}.\text{s}^{-1}$) is the viscosity of nanofluid, p (N.m^{-2}) is

the pressure, T (K) is temperature, k_{nf} ($\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) is the thermal conductivity of nanofluid, and C_{pnf} ($\text{J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$) is the heat capacity of nanofluid. The properties of the nanofluid are calculated using the following equation:

$$\rho_{nf} = (1 - \phi)\rho_f + \phi\rho_s \quad (6)$$

$$C_{pnf} = (1 - \phi)C_{pf} + \phi C_{ps} \quad (7)$$

where the subscripts f and s stands for fluid and solid respectively. For effective thermal conductivity, there are few conventional equations such as Hamilton-Crosser [4] Maxwell [4]. For viscosity, there are also some conventional equations such as Einstein's [5], Brickman [5]. He et al [7] derived the following equations for viscosity and thermal conductivity, which are adopted in the present study.

Nanofluid thermal conductivity:

$$k_{nf} = (125.62\phi^2 + 4.82\phi + 1)k_f \quad (8)$$

Nanofluid viscosity:

$$\mu_{nf} = (199.21\phi^2 + 4.62\phi + 1)\mu_f \quad (9)$$

where ϕ is in percentage of volume fraction = volume of the nano-particles/total volume, ρ_f is the density of base fluid, ρ_s is the density of nanoparticle, C_{pf} is the heat capacity of base fluid, C_{ps} is the heat capacity of nanoparticle, k_f is the thermal conductivity of base fluid, μ_f is the viscosity of base fluid. The properties of the nanofluid components used in the present study are given in Table 1 [4][11].

Table 1: Properties of the TiO_2 nano particles [4][11].

Properties	Air	Water	TiO_2 Particles
Density, ρ ($\text{kg}\cdot\text{m}^{-3}$)	1.03	997.746	4850
Specific heat Capacity, C_p ($\text{J}\cdot\text{Kg}^{-1}\cdot\text{K}^{-1}$)	1009	4180.2	544.25
Thermal conductivity, k ($\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$)	0.0241	0.60192	7.44
Dynamic viscosity, μ ($\text{kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$)	1.94×10^{-5}	0.96172×10^{-3}	-

3. NUMERICAL METHOD AND VALIDATION TESTS

The solution domain is considered as two regions. The inner region is the horizontal pipe with negligible thickness. The pipe is subjected to an external cross flow in a duct, which represents the outer region. The nanofluid is flowing inside the pipe and a pure air is flowing in the duct across the pipe. The air duct is meshed by splitting the total volume into 3 volumes as shown in Fig. 1. Air duct is meshed using element of hex/wedge with copper type. For the pipe, boundary layer mesh is produced with the setting of first row at 0.01mm, growth factor = 1.1, rows = 15 with 96 mesh edge at θ direction and 28 mesh edge at radial direction. The

face is then mesh using tri element with pave type. This is to ensure that the mesh spacing gradually increase from wall to centre of pipe. Specific continuums are created for both volumes of air and water.

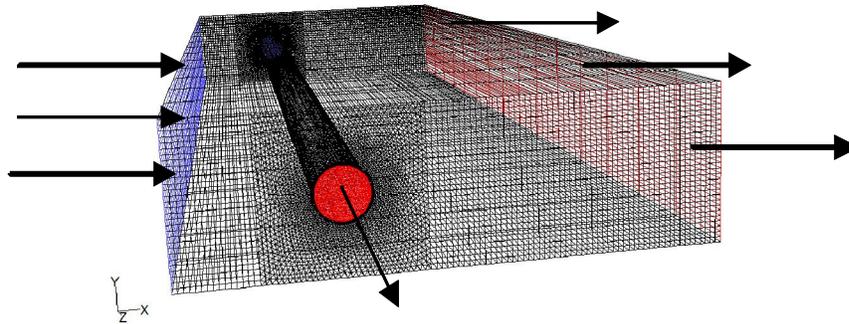


Fig. 1: Mesh geometry for internal and external domains.

Dimensions (Air Duct = 100mm×30mm×300mm; pipe radius =5mm and length =300mm)

Fluent 6.3 [12] is used as a tool for numerical solution of the governing equations based on finite-volume method. The governing equations were discretized using QUICK scheme for convection-diffusion formulations with SIMPLEC velocity-pressure coupling algorithm. Convergence is satisfied with a minimum residual of 10^{-5} . Initial temperature for water is set to 293 K and for air it is set to 323K. Initial velocity for both cross flow and normal flow is calculated from the desired Re. In all the following simulations the Reynolds number for the internal and external flows is based on the pipe diameter and has the same value which is selected to be in the laminar flow regime. To test the present numerical method, the results are compared with the results of the pure water flow in pipes and external air flow across the pipe. The performance of the cross flow heat exchanger is evaluated based on the calculation of the Nusselt number, which is defined as:

$$Nu = \frac{hD}{k_{nf}} \quad (10)$$

where D is the diameter of the pipe, k_{nf} is the thermal conductivity of the nanofluid and h is the local heat transfer coefficient calculated from $h = q_w / (T_w - T_{av})$ where q_w is the heat flux at the wall of the pipe, T_w is the wall temperature and T_{av} is the average temperature across tube diameter.

The comparison of the variation of Nusselt number along the pipe with different references at Re= 900 is shown in Fig. 2a for pure water flow. For the air flow across the pipe, Fig. 2b shows the comparison of mean Nu around the cylinder surface with NACA [13] experiment result with Re= 38900. In this case a turbulence model is needed since the Reynolds number is high. The k- ϵ - ω turbulence model [12] is used to generate the results depicted in Fig. 2b.

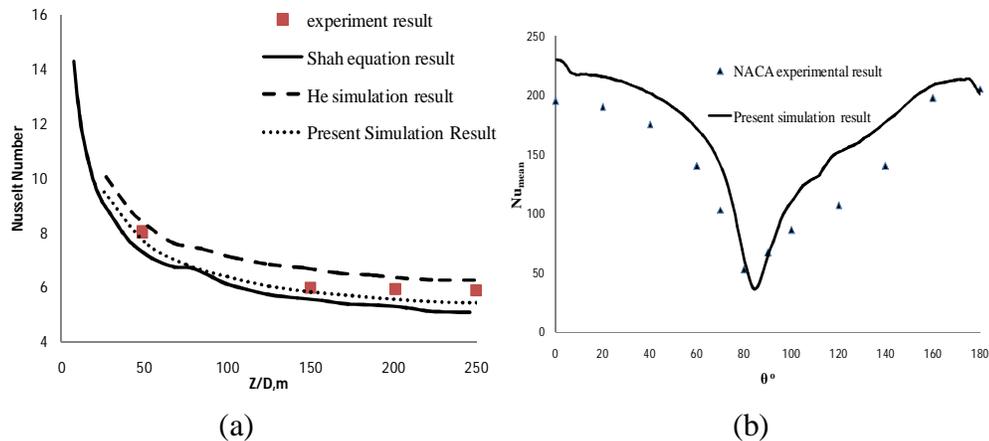


Fig. 2: (a) Variation of Nu along the pipe with $Re= 900$ for pure water [7][8], (b) Comparison of mean Nu around the cylinder surface with NACA [11] experiment result with $Re= 38900$.

In Fig. 2(a), it can be seen that the trend of simulated results with $Re=900$ is almost same as the experiment result, He et al. [7] simulation and Shah's equation [8]. The present simulation results for pure water show that the Nusselt number at the end of the pipe is 5.43. The difference in the values of Nu between the present results and the experimental result is about 7.7%. This difference in Nu at outlet of the pipe is about 6.63 compared with He et al [7] simulation results. Therefore, it can be conclude that the simulation is validated. The results presented in Fig. 2(b) show the accuracy of the present numerical method to predict the mean Nusselt number around the surface of the cylinder in cross flow situation compared with NACA [13] experimental results.

4. RESULTS AND DISCUSSION

Parametric study is carried out by varying Reynolds number of the water in the range 500,1000, 1500 and 2000 and nano-fluid volume fraction in the range of $\phi = 0.6\%$, 1.5%, 3%, 6% and 10%. Figures 3(a) and 3(b) show the Nusselt number record highest increment at the inlet due to large temperature difference and gradually decrease and come to a constant at the fully developed region. Furthermore, from Fig 3(a), heat transfer coefficient increases as Reynolds number increase with a constant volume fraction of TiO_2 0.6%. On the other hand, heat transfer also increase as volume fraction of TiO_2 increases at constant Reynolds number $Re=1000$ as shown in Fig 3(b). The increment of volume fraction from 0.6%-1.5% has recorded enhancement of Nusselt number at about 6.5%. This happens because thermal conductivity of the nanofluid is increased from $0.62205 \text{ (W.m}^{-1}.\text{K}^{-1})$ to $0.66452 \text{ (W.m}^{-1}.\text{K}^{-1})$ as volume fraction increase.

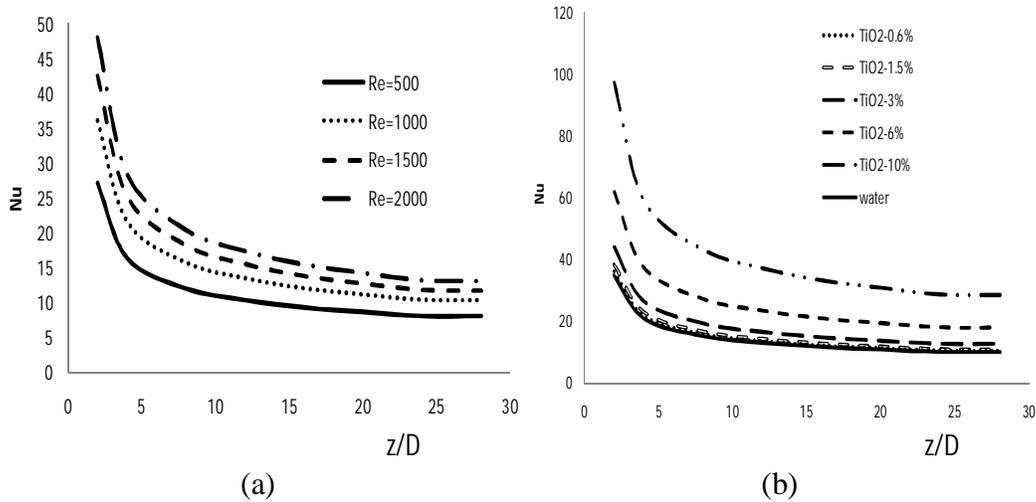


Fig. 3: Nusselt number variation along the pipe with (a) different Reynolds numbers, (b) different volume fractions of TiO₂ nano-fluid at Re=1000.

Figure 4(a) shows that the Nusselt number increases as the Reynolds number increases. The value of Nusselt number is about 139.515 at Re = 2000 which is about 49% higher than that at Re = 500. This is due to the separation happens at about 120° for Re = 500 and it happens at about 98° as Reynolds number increases to Re = 2000. The results presented in Fig. 4(b), shows that the Nusselt number increases as volume fraction of nano-fluid TiO₂ increase. The Nusselt number for each volume fraction comes to a minimum value at angle of about 108° due to separation of the flow. Beyond this angle to 180°, the values of the Nusselt number show slight increment. Hence, most of the heat transfer is occur between 0-100°.

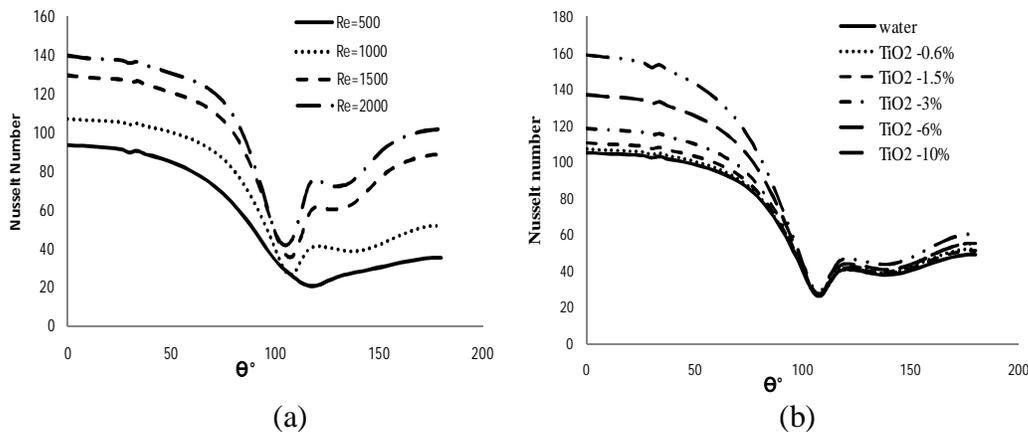


Fig. 4: Nusselt number variation at mid-span of cylinder with (a) TiO₂ of volume fraction 0.6% flow at different Reynolds numbers, (b) different volume fractions of TiO₂ nano-fluid at with Re=1000.

Finally, the isotherms for both inner and outer regions are shown in Fig. 5. These results are generated for laminar cross flow of hot air over a pipe of nano-fluid (0.6% TiO₂ – water) flow with Re = 1000. The inlet conditions are as follows: inlet water temperature 295K, inlet

water velocity 0.0974 m/s, inlet air temperature 323K, inlet air velocity 1.8835 m/s. The isotherms for the internal pipe flow show the increase of the water temperature as the hot air flow over the pipe. On the external air side the isotherms which indicate the separation point are shown at inlet, outlet, and mid-span across the pipe.

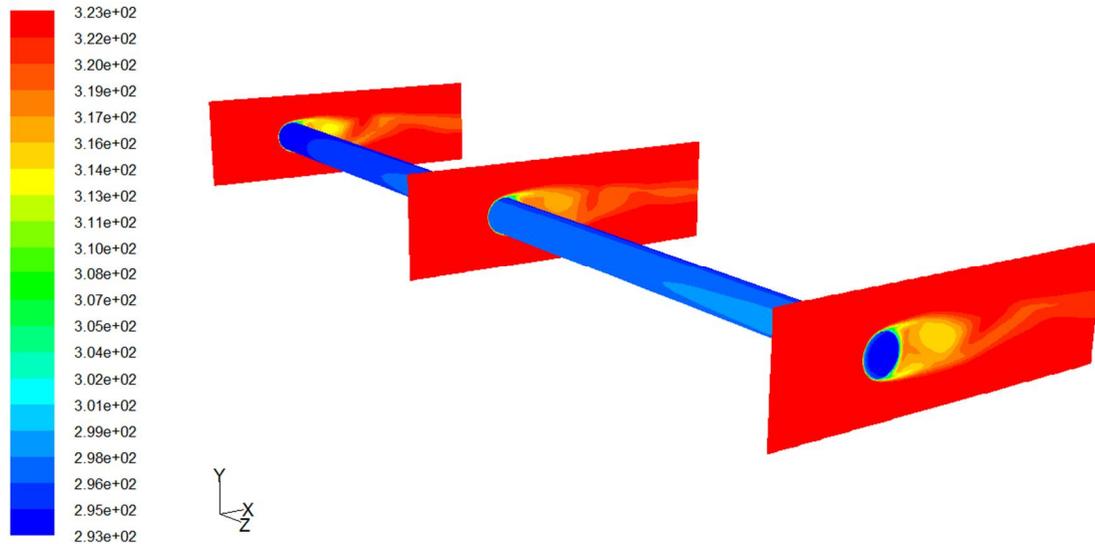


Fig. 5: Isotherms for inner and outer regions at $Re = 1000$ for 0.6% TiO_2 water nanofluid.

5. CONCLUSIONS

The present simulation results show that the convective heat transfer process can be significantly improved by introducing nano-particles such as TiO_2 in base fluid. The present simulation results show the enhancement in the convection heat transfer by either increase the Reynolds number or the nano-particles volume fraction. However, higher volume fraction will cause higher wall shear stress which may need more energy to pump the nano-fluid in the cylindrical pipe and also may cause abrasion of the cylinder wall which causes corrosion, scaling, and clogging of the pipe. The accuracy of the present results depends on the accuracy of the effective properties of the nano-fluids, which are taken from the open literature.

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